

Factoring Simple Quadratic Trinomials ($x^2 + bx + c$)

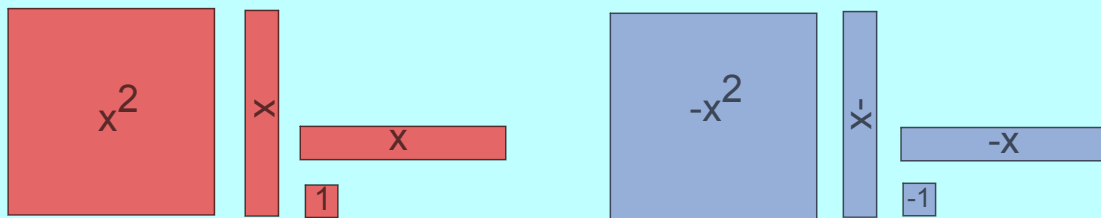
March 24/2011

1. Using Alge-tiles

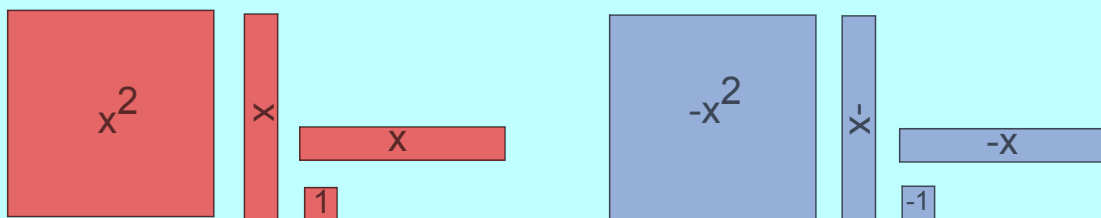
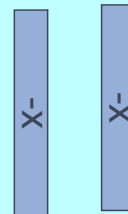
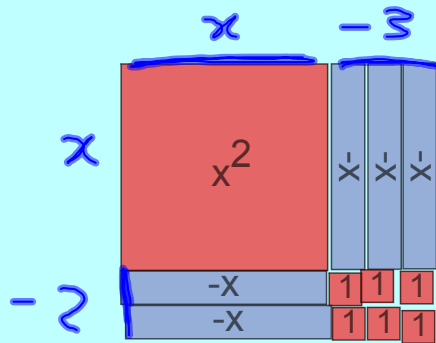
Model the expression as an area. The tiles must form a rectangle (or square).

The lengths of the sides are factors.

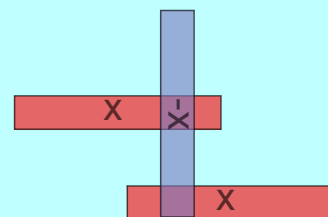
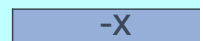
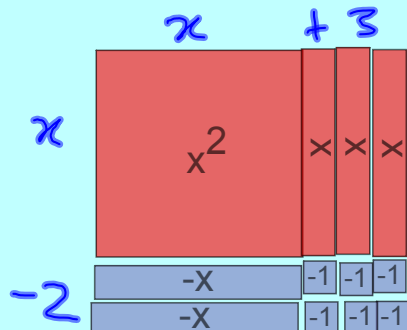
Factor: $x^2 + 4x + 3 = (x+3)(x+1)$



Factor: $x^2 - 5x + 6 = (x-3)(x-2)$



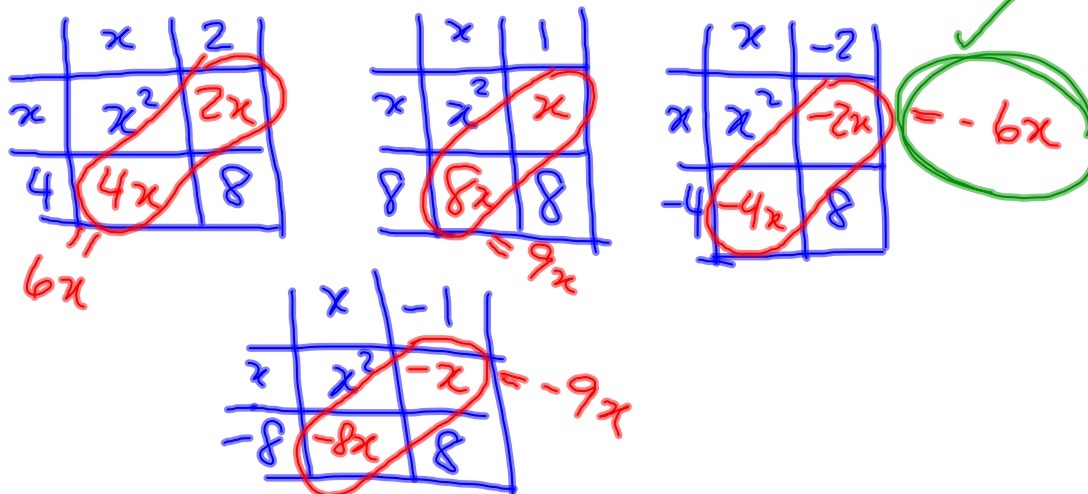
Factor: $x^2 + x - 6 = (x+3)(x-2)$



2. Using a Diagram

What are the possible dimensions of the constant value (bottom right corner)?

Ex. Factor $x^2 - 6x + 8 = (x-2)(x-4)$



3. Algebraically

Consider: $(x + 2)(x + 3) = x^2 + 5x + 6$

What relationship is there between the factors and the coefficients of the answer?

$2 + 3 = 5 \rightarrow$ middle term is the sum of factors

$2 \times 3 = 6 \rightarrow$ constant term is the product of the factors

In general, given

$$(x + m)(x + n) = x^2 + bx + c$$

then

$$b = m + n \quad \text{and} \quad c = m \times n$$

To factor $x^2 + bx + c$:

1. Find two numbers that multiply to c , and
2. the same two numbers that add to b .

constant term



middle term



Ex. Factor $x^2 - 8x + 12$

what multiplies to 12?

$$x^2 - 8x + 12$$

$$= (x - 6)(x - 2)$$

3, 4

6, 2

1, 12

-3, -4

-6, -2

-1, -12

add

7 x

8 x

13 x

-7 x

-8 ✓

-13 x

Assigned Work:

p.211-213 #~~1~~, 2b, 3bc, 4, 7, 8,
#9 (look for common factors first)
#12