
 Transformations of Relations

Yesterday we reviewed the transformations that you studied in grade 10.

Recall: Reflection along the x -axis: $y = ax^2$, $a < 0$ or in function notation: $y = af(x)$, where $f(x) = x^2$.

Vertical Scaling: $y = ax^2$, $a > 0$ or in function notation: $y = af(x)$, where $f(x) = x^2$.
vertical stretch: $a > 1$ (parabola gets skinnier)
or vertical compression: $0 < a < 1$ (parabola becomes wider)

Vertical Translation: $y = x^2 + q$ or in function notation: $y = f(x) + q$, where $f(x) = x^2$.
vertical shift up: $q > 0$ (parabola moves up)
or vertical shift down: $q < 0$ (parabola moves down)

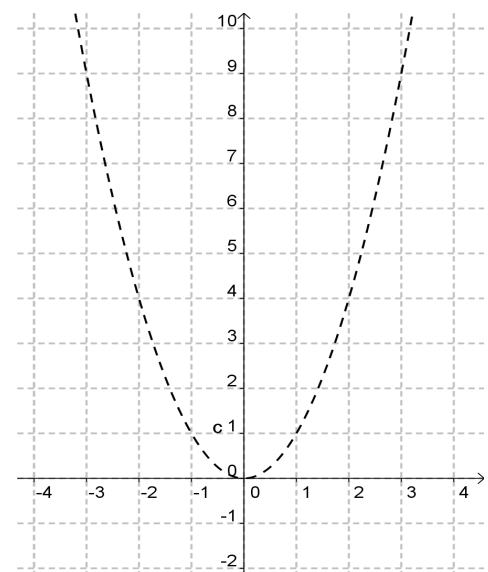
Horizontal Translation: $y = (x - p)^2$ or in function notation: $y = f(x - p)$, where $f(x) = x^2$.
horizontal shift right: $p > 0$, like in $y = (x - 3)^2$
or horizontal shift left: $p < 0$, like in $y = (x + 2)^2$

Ex: State the transformations, in the appropriate order, that $y = f(x)$ has undergone to obtain $y = f(x - 1) + 3$

Using the example above, what if the parent function is a quadratic? Then $f(x) = x^2$.

Sketch the transformed parabola on the grid below.

(Use a table of values if you want to!)



What if the parent function is a set of ordered pairs? If $f(x) = \{(1,2), (2,-3), (-5,7)\}$?

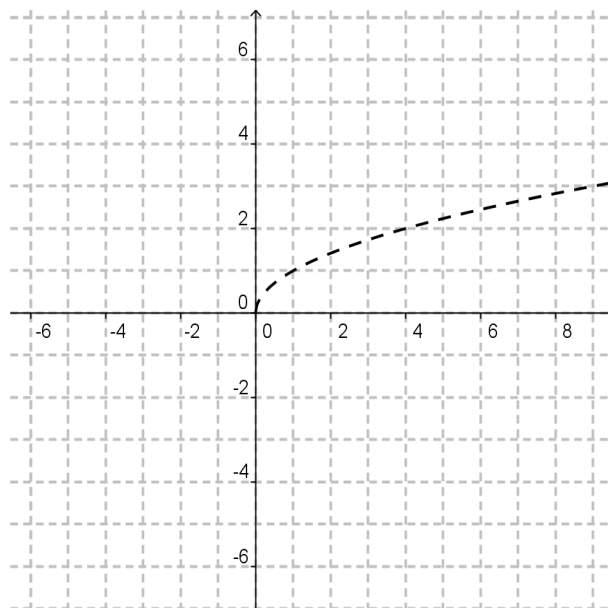
What would $y = f(x-1) + 3$ be?

(Use a table of values and/or graph if you want to!)

What if the parent function is the square root function?

Then $f(x) = \sqrt{x}$. What would $y = f(x-1) + 3$ be?

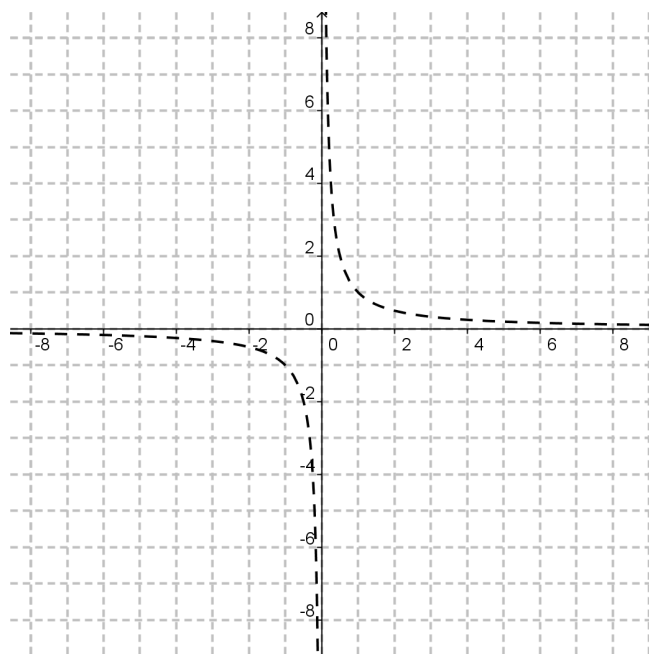
(Use a table of values and/or graph if you want to!)



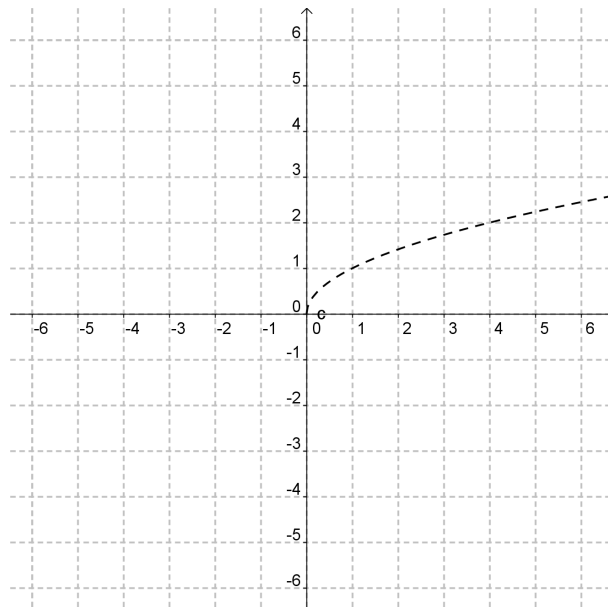
What if the parent function is the reciprocal function?

Then $f(x) = \frac{1}{x}$. What would $y = f(x-1) + 3$ be?

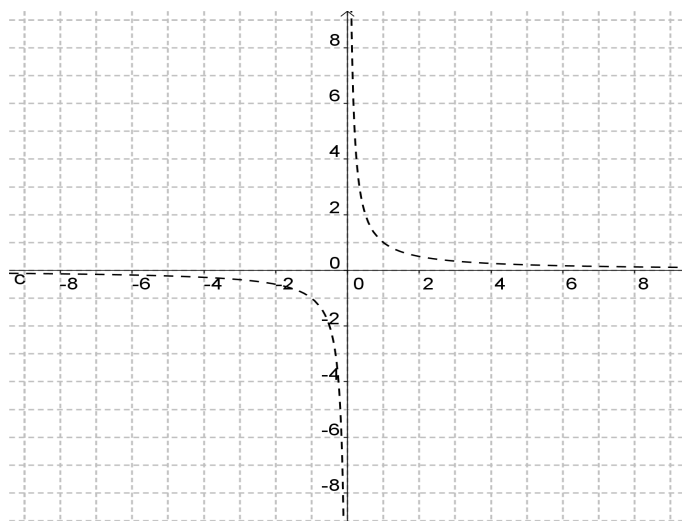
(Use a table of values and/or graph if you want to!)



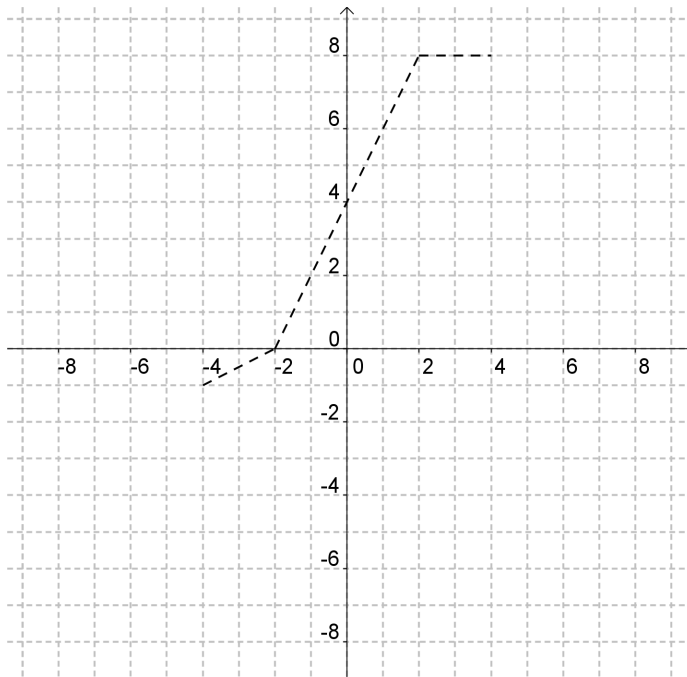
Ex: Given $y=2f(x)+3$ describe the transformations and apply them to the square root function.
 (Use a table of values and/or graph if you want to!)



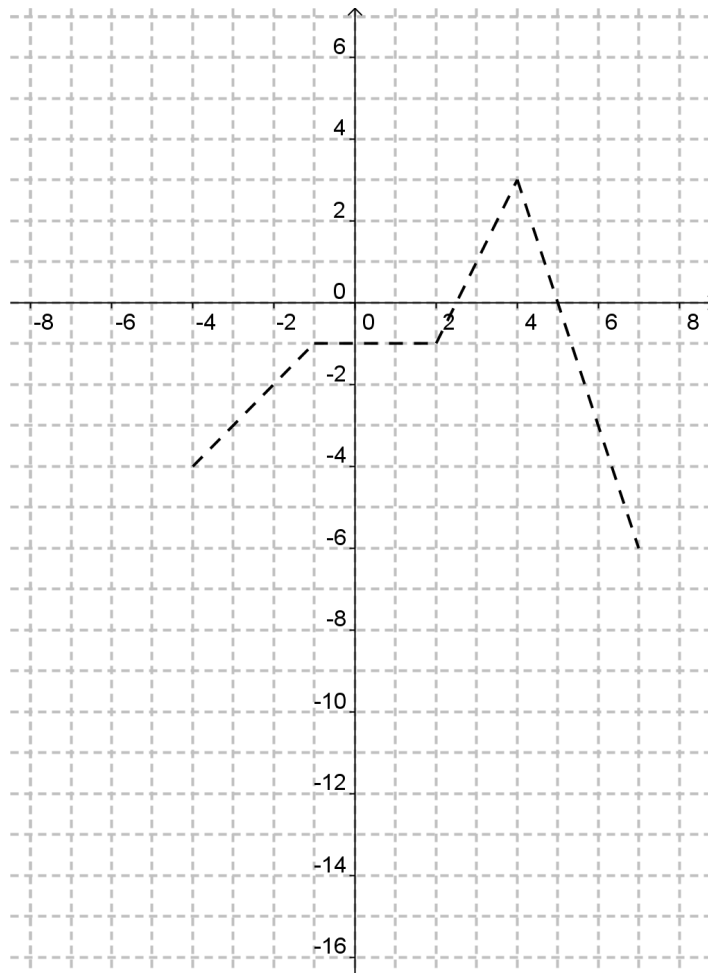
Ex: Given $y=0.4f(x+1)$ describe the transformations and apply them to the reciprocal function.
 (Use a table of values and/or graph if you want to!)



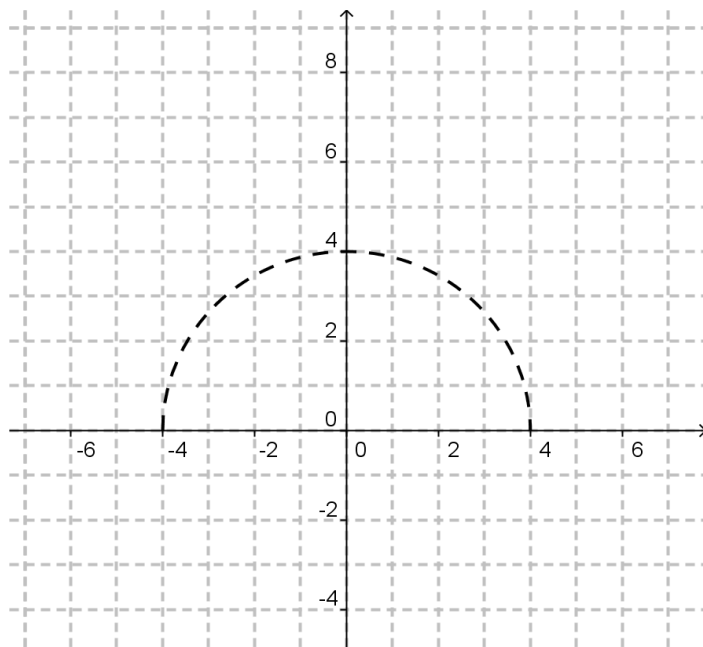
Ex: The graph on the right shows the function $y=f(x)$. Given $y=-f(x+1)-2$, describe the transformations and apply them to the function
 (Use a table of values with the key points, if you want to!)



Ex: The graph on the right shows the function $y=f(x)$. Given $y=2f(x)-1$, describe the transformations and apply them to the function. (Use a table of values with the key points, if you want to!)



Ex: The graph on the right shows the function $f(x)=\sqrt{16-x^2}$. Given $y=-0.5f(x+2)$, describe the transformations and apply them to the function. (Use a table of values with the key points, if you want to!)



HW: Pg. 241 #8b, 9b, 5abd, 4abce