

Triangle Centres

March 8/2010

Recall: There is more than one centre for triangles.

The **centroid** is the intersection point of the **medians**.

The **orthocentre** is the intersection point of the **altitudes**.

The **circumcentre** is the intersection point of  
the **perpendicular bisectors**.

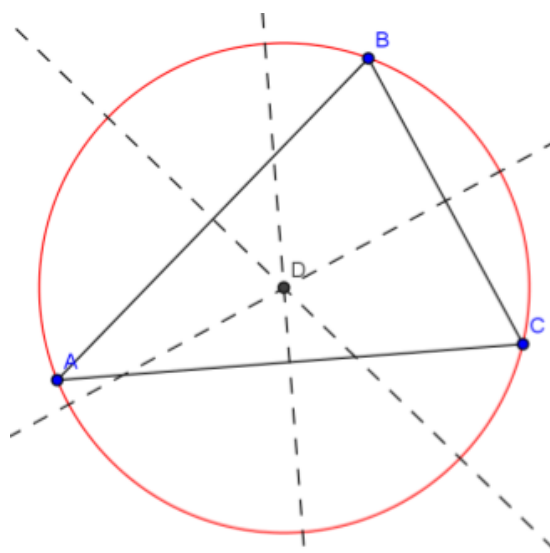
The **incentre** is the intersection point of  
the **angle bisectors**.

The **centroid** is also known as the centre of mass of the triangle. You could balance the triangle at this point.

The **circumcentre** is the point that is equidistant from all 3 vertices of the triangle.

or

It is the centre of the circle that passes through each vertex of the triangle.

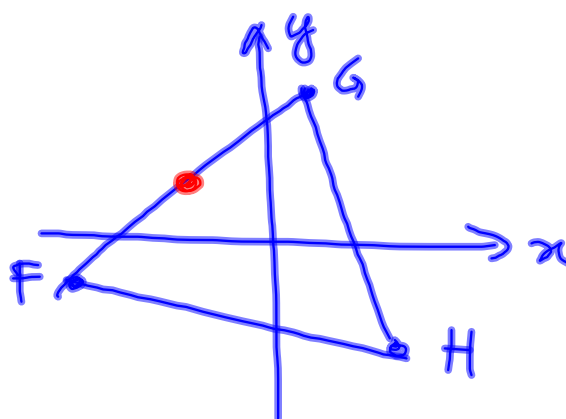


Ex.1. Given triangle FGH with vertices at  $F(-7,-1)$ ,  $G(1,6)$ , and  $H(3,-4)$ :

- a) List the steps required to determine the coordinates of the circumcentre, and then find it. (draw a sketch first!)
- b) List the steps required to determine the coordinates of the centroid, and then find it. (draw a sketch... maybe a new one)

Ex.1. Given triangle FGH with vertices at  $F(-7,-1)$ ,  $G(1,6)$ , and  $H(3,-4)$ :

(a) circumcentre  
 $\rightarrow$  intersect  
 $\perp$ -bisectors  
*\* only need 2.*

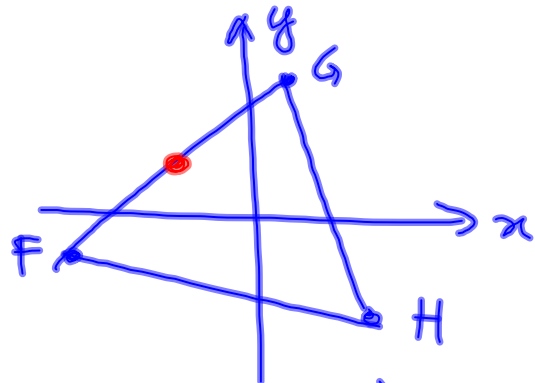


- (A)  $\perp$ -bisector for FG
- ① MP of FG
  - ② slope of FG
  - ③  $\perp$  slope
  - ④ y-int
- (B)  $\perp$ -bisector of FH
- $\rightarrow$  Same Steps

Ex.1. Given triangle FGH with vertices at F(-7,-1), G(1,6), and H(3,-4):

FG

$$\begin{aligned} \textcircled{1} \quad x_m &= \frac{x_1 + x_2}{2} \\ &= \frac{-7 + 1}{2} \\ &= -3 \\ y_m &= \frac{y_1 + y_2}{2} \\ &= \frac{-1 + 6}{2} \\ &= \frac{5}{2} \end{aligned}$$



$\therefore$  MP of FG is  $(-3, \frac{5}{2})$

$$\begin{aligned} \textcircled{2} \quad \text{slope FG} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{6 - (-1)}{1 - (-7)} \\ &= \frac{7}{8} \end{aligned} \quad \begin{aligned} \textcircled{3} \quad \perp \text{ slope} \\ m_{\perp} &= -\frac{8}{7} \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad y\text{-int} \quad y &= -\frac{8}{7}x + b \\ \text{Sub } (-3, \frac{5}{2}): \quad \frac{5}{2} &= -\frac{8}{7}(-3) + b \end{aligned}$$

$$\frac{5}{2} = \frac{24}{7} + b$$

$$\frac{5}{2} - \frac{24}{7} = b$$

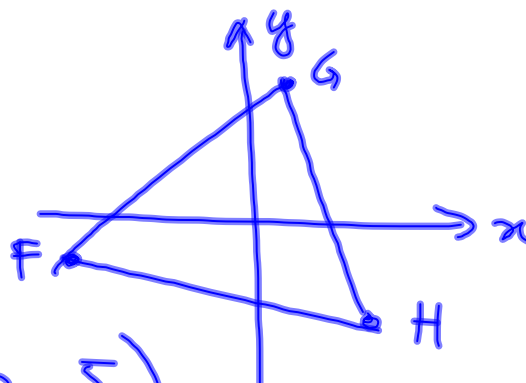
$$\frac{35}{14} - \frac{48}{14} = b$$

$$-\frac{13}{14} = b$$

$\therefore$   $\perp$ -bisector  
of FG is

$$y = -\frac{8}{7}x - \frac{13}{14}$$

Ex.1. Given triangle FGH with vertices at F(-7,-1), G(1,6), and H(3,-4):



$$\begin{aligned} &\text{FH} \\ \textcircled{1} \quad x_m &= \frac{-7+3}{2} \\ &= -2 \\ y_m &= \frac{-1+(-4)}{2} \\ &= -\frac{5}{2} \end{aligned} \quad \left(-2, -\frac{5}{2}\right)$$

$$\begin{aligned} \textcircled{2} \quad m_{FH} &= \frac{-4-(-1)}{3-(-7)} \\ &= \frac{-3}{10} \end{aligned} \quad \textcircled{3} \quad m_{\perp} = \frac{10}{3}$$

$$\frac{10}{-3} \xrightarrow{x-1} \frac{10}{3}$$

$$\textcircled{4} \quad y = \frac{10}{3}x + b \quad \text{sub } \left(-2, -\frac{5}{2}\right)$$

$$-\frac{5}{2} = \frac{10}{3}(-2) + b$$

$$-\frac{5}{2} = -\frac{20}{3} + b$$

$$-\frac{15}{6} + \frac{40}{6} = b$$

$$\frac{25}{6} = b$$

$\therefore$   $\perp$ -bisector  
of FH is

$$y = \frac{10}{3}x + \frac{25}{6}$$

Assigned Work:

p.195 # 6, 8, 10