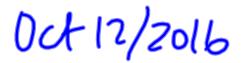
## Rates of Change in Polynomial Functions



Recall:

(1) Average rate of change between x = a and x = b is the slope of the secant line:

$$m_{\text{secant}} = \frac{f(b) - f(a)}{b - a}$$

(2) Instantaneous rate of change is the slope of the tangent line at x = a, but can only be estimated:

$$m_{\text{tangent}} = \frac{f(a+h) - f(a)}{h}$$

Improve the estimate by choosing smaller values of h.

When estimating instantaneous rate of change, how do we know if our estimate is "good enough"?

We need at least two estimates to compare against each other. Ideally, there will be an obvious trend, which we can use as our final estimate.

$$\%$$
diff =  $\left| \frac{\text{accepted - estimate}}{\text{accepted}} \right| \times 100\%$ 

Since we do not know the final, correct value, use your best estimate as "accepted".

Ex.1 Estimate the iRoC at x = 4 to within 1%, for the polynomial

$$f(x) = 2(x-3)(x-2)(x+5)$$

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$$f(x) = 2(x-3)(x-2)(x+5)$$

(1)  $a = 4$ ,  $b = 0.1$ 
 $f(4)$ 
 $f(4)$ 

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Some important rates of change

- rate of change of distance is speed
  - rate of change of speed is acceleration

rate of

At a turning point (maximum or minimum), the instantaneous change (slope on graph) will be zero.

Assigned Work:

p.235 # 5cde, 6cde, 7, 9 11

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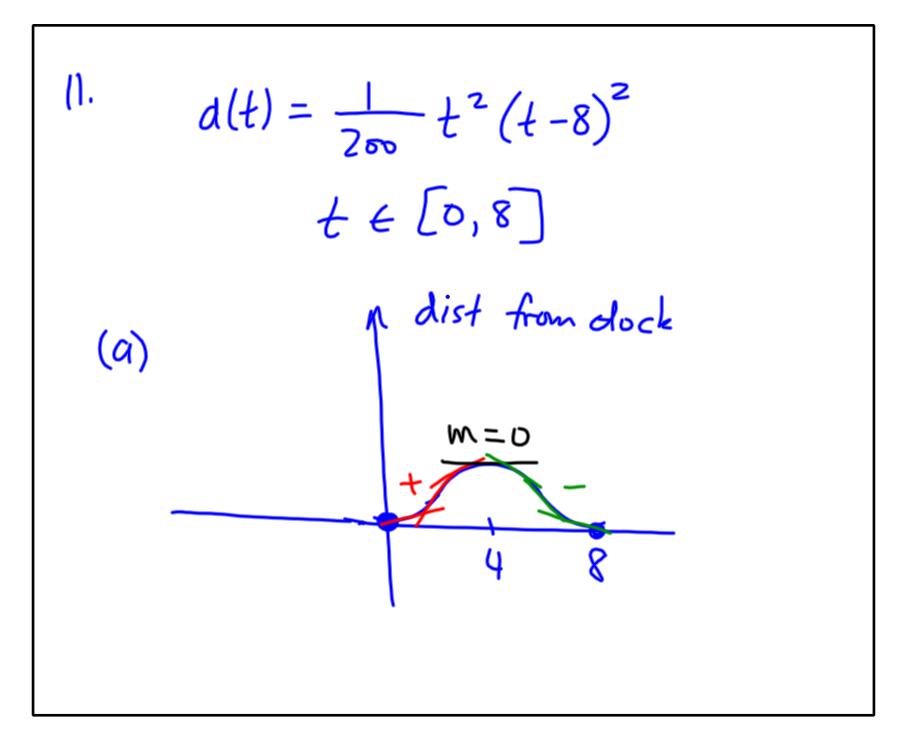
9. 
$$f(x) = 3x^2 - 4x - 1$$

(a)  $M_{1} = 2$ 

(b)  $(a, f(a))$ 

$$= (1, f(1))$$

$$= (1, -2)$$



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