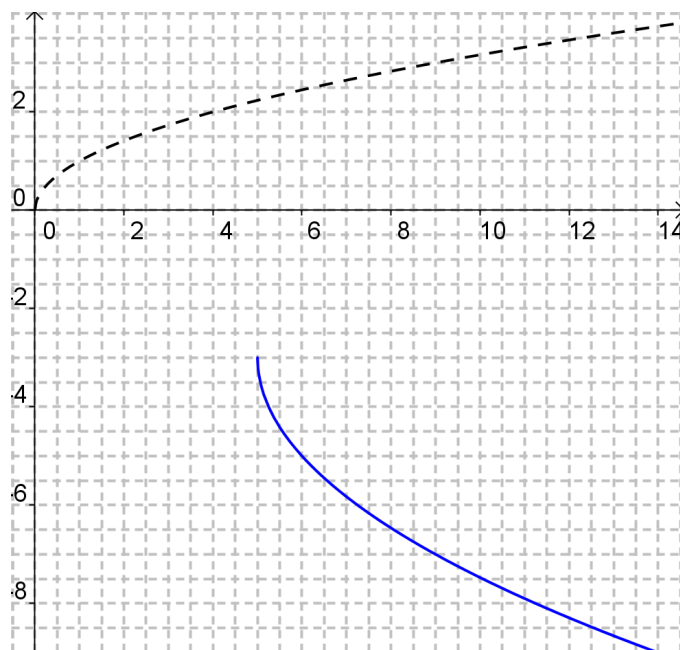


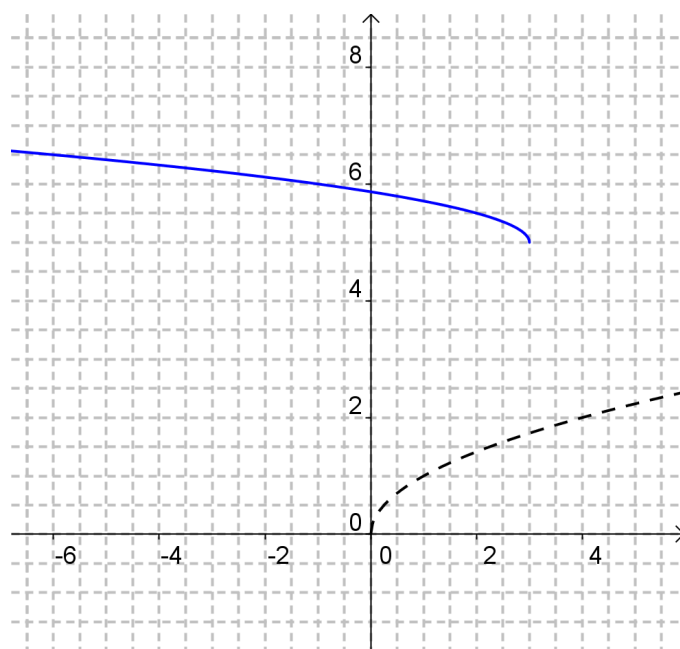
Ex.1 The diagram below shows a transformed radical function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- $(0,0) \rightarrow (5,-3)$: $p=5$ and $q=-3$
- vertical reflection: $a < 0$
- for radical function, choose to look only at k , so $|a|=1$ and $a=-1$
- looks like a horizontal compression, so try to find where the point $(4,2)$ has moved on the new graph
 - choose $(4,2)$ because it's a compression, so start with a bigger x-value (4) and see how much smaller it gets
 - the y-value (2) will be the same
 - a step of 4 in the x becomes a step of 1
 - $|k|=4$ (compression by 4)
- $y = -f[4(x-5)] - 3$



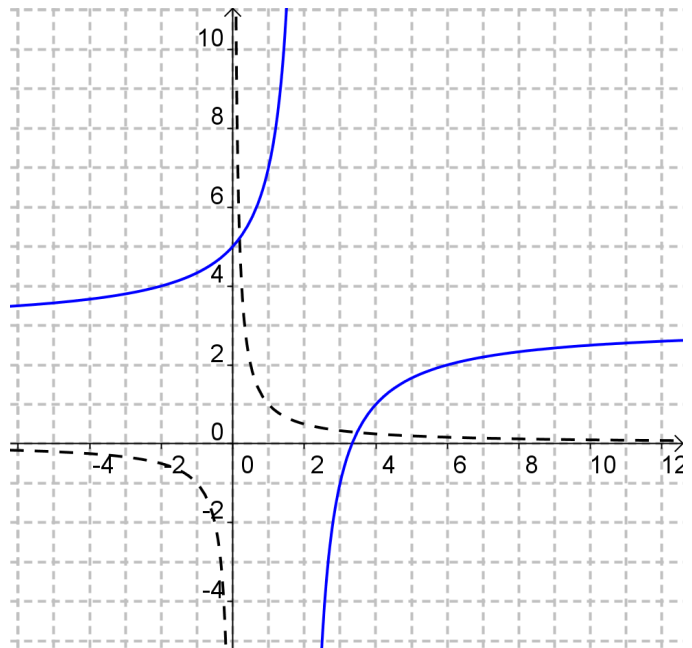
Ex.2 The diagram below shows a transformed radical function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- $(0,0) \rightarrow (3,5)$: $p=3$ and $q=5$
- horizontal reflection: $k < 0$
- for radical function, choose to look only at k , so $|a|=1$ and $a=-1$
- looks like a horizontal stretch, so try to find where the point $(1,1)$ has moved on the new graph
 - choose $(1,1)$ because it's a stretch, so start with a smaller x-value (1) and see how much bigger it gets
 - the y-value (1) will be the same
 - a step of 1 in the x becomes a step of 4
 - $|k| = \frac{1}{4}$ (stretch by 4)
- $y = f\left[-\frac{1}{4}(x-3)\right] + 5$



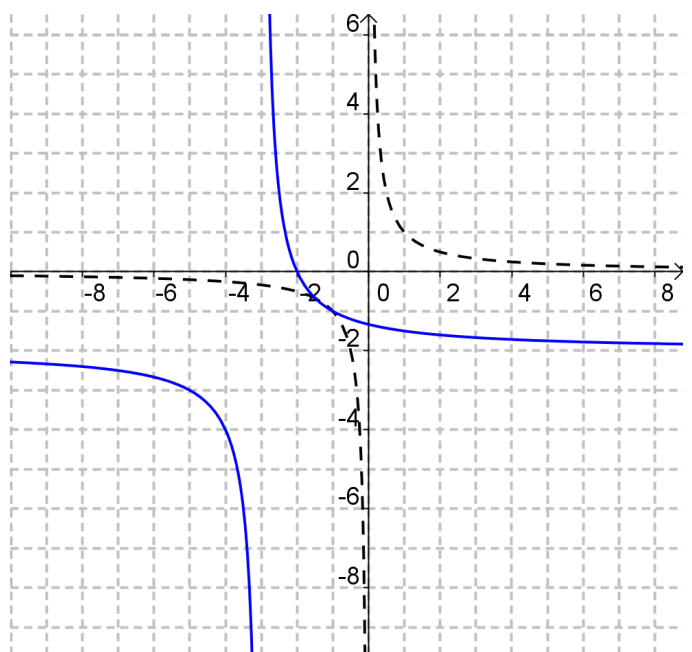
Ex.3 The diagram below shows a transformed reciprocal function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- asymptotes: $x=0 \rightarrow x=2$ and $y=0 \rightarrow y=3$
 $p=2$ and $q=3$
- for reciprocal, either reflection is fine
 - choose vertical reflection: $a < 0$
- for reciprocal, either scaling is fine
 - choose vertical scaling, so $k=1$
- consider vertical distance from asymptote to point $(1,1)$, so $d_1=1$
- now consider vertical distance from new asymptote ($y=3$) to new point $(1,-1)$
 - remember to measure distance from asymptote, which is $d_2=4$
- vertical stretch by 4, $|a|=4$, $a=-4$
- $y = -4 f(x-2) + 3$



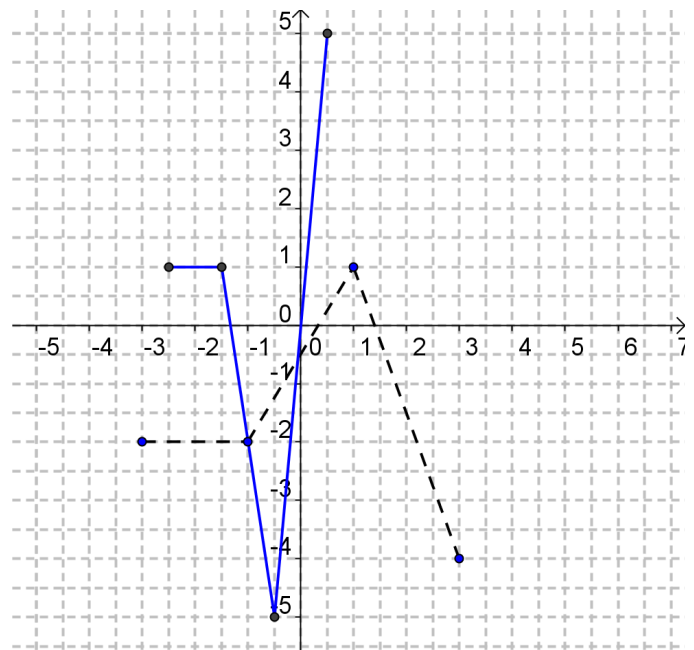
Ex.4 The diagram below shows a transformed reciprocal function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- asymptotes: $x=0 \rightarrow x=-3$ and $y=0 \rightarrow y=-2$
 $p=-3$ and $q=-2$
- no reflection
- for reciprocal, either scaling is fine
 - choose vertical scaling, so $k=1$
- consider vertical distance from asymptote to point $(1,1)$, so $d_1=1$
- now consider vertical distance from new asymptote ($y=-2$) to new point $(-2,0)$
 - remember to measure distance from asymptote, which is $d_2=2$
- vertical stretch by 2, $|a|=2$, $a=2$
- $y = 2 f(x+3) - 2$



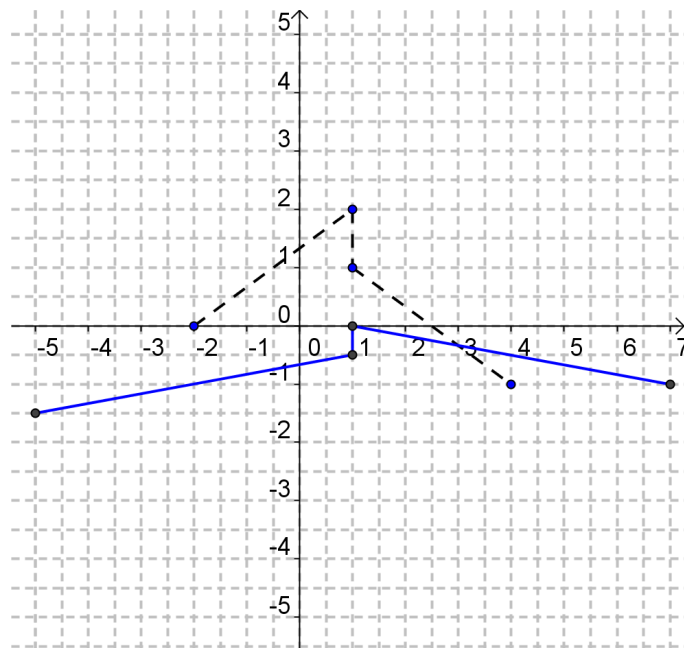
Ex.5 The diagram below shows a transformed piecewise function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- no well-defined zero-values to work with
- vertical reflection
- compare full-widths and full-heights
- $w_1=6$, $w_2=3$
 - compress by 2, $|k|=2$, $k=2$
- $h_1=5$, $h_2=10$
 - stretch by 2, $|a|=2$, $a=-2$
- use $(x, y) \rightarrow \left(\frac{x}{k} + p, a y + q\right)$ to find p, q
 - $(1, 1) \rightarrow (-0.5, -5)$
 - $\frac{1}{2} + p = -0.5$, $p = -1$
 - $-2(1) + q = -5$, $q = -3$
- $y = -2 f[2(x+1)] - 3$



Ex.6 The diagram below shows a transformed piecewise function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- $(-2, 0) \rightarrow (7, -1)$ so $q = -1$
- horizontal reflection, $k < 0$, $a > 0$
- compare full-widths and full-heights
- $w_1=6$, $w_2=12$
 - h. stretch by 2, $|k|=\frac{1}{2}$, $k=-\frac{1}{2}$
- $h_1=3$, $h_2=1.5$
 - compress by 2, $|a|=\frac{1}{2}$, $a=\frac{1}{2}$
- use $(x, y) \rightarrow \left(\frac{x}{k} + p, a y + q\right)$ to find p
 - $(1, 1) \rightarrow (1, -0.5)$
 - $-2x + p = 1$
 - $-2(1) + p = 1$
 - $p = 3$
- $y = \frac{1}{2} f\left[-\frac{1}{2}(x-3)\right] - 1$

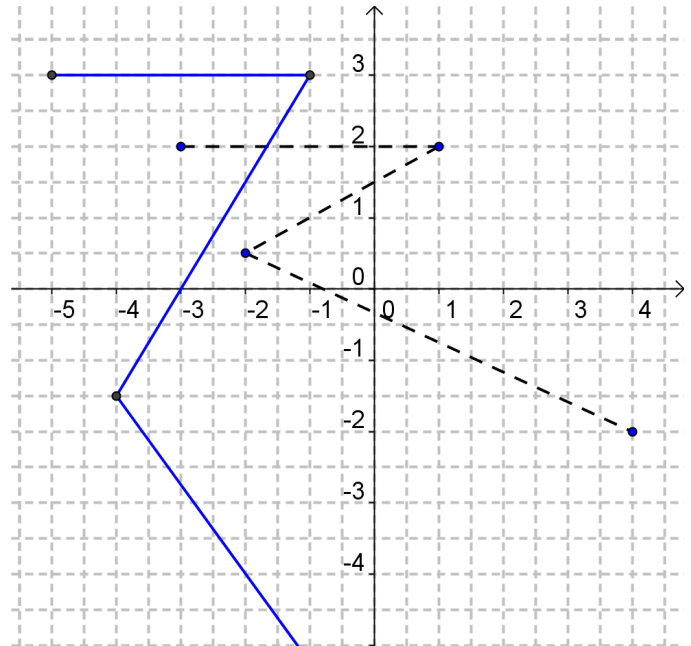


Ex.7 The diagram below shows a transformed piecewise function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- no zero-values to work with
- no reflections, $k > 0$, $a > 0$
- one point missing, so compare widths and heights between key points
- top 2 points: $w_1 = 4$, $w_2 = 4$, $k = 1$
- 2nd & 3rd points: $h_1 = 1.5$, $h_2 = 4.5$
 - v.stretch by 3, $|a| = 3$, $a = 3$
- use $(x, y) \rightarrow \left(\frac{x}{k} + p, ay + q\right)$ to find p, q
 - $(1, 2) \rightarrow (-1, 3)$

$$\begin{array}{rcl} x + p & = & -1 \\ (1) + p & = & -1 \end{array} \quad \begin{array}{rcl} 3y + q & = & 3 \\ 3(2) + q & = & 3 \end{array}$$

$$\begin{array}{rcl} p & = & -2 \\ q & = & -3 \end{array}$$
- $y = 3f(x + 2) - 3$



Ex.8 The diagram below shows a transformed piecewise function as well as the parent function. Determine the transformations involved and express the entire transformation using function notation.

- $(0, 4) \rightarrow (2, 3)$: right 2, $p = 2$
- $(-6, 0) \rightarrow (4, 5)$: up 5, $q = 5$
- difficult to see (sorry), but there is actually a vertical and horizontal reflection: $k < 0$, $a < 0$
- compare width: $w_1 = 9$, $w_2 = 3$
 - h.compress by 3: $|k| = 3$, $k = -3$
- compare height: $h_1 = 7$, $h_2 = 3.5$
 - v.compress by 2: $|a| = 2$, $a = -2$
- $y = \frac{-1}{2}f[-3(x - 2)] + 5$

