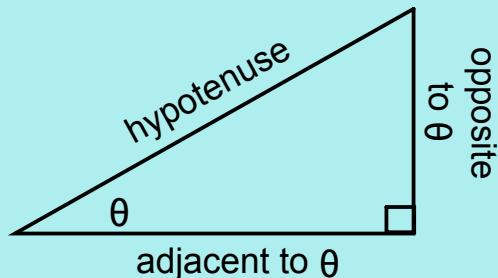


For any angle of interest, there are three (3) primary trigonometric ratios.

$$\text{sine of } \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\text{cosine of } \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\text{tangent of } \theta = \frac{\text{opposite}}{\text{adjacent}}$$



S o h C a h T o a

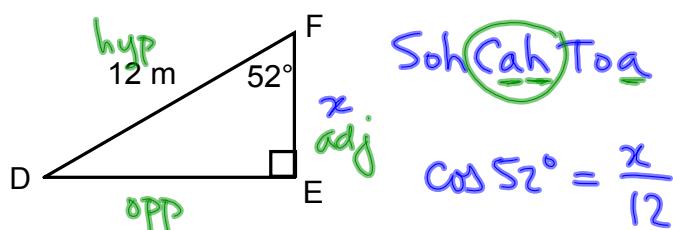
Dec 7-9:58 PM

### Solving Right Triangles

Dec 12/2011

Recall: Trigonometric ratios can be used to determine side lengths or angle measures.

Ex. 1 Calculate the height of the triangle shown below.



$$\cos 52^\circ = \frac{x}{12}$$

$\therefore$  height of  
Δ is 7.4m.

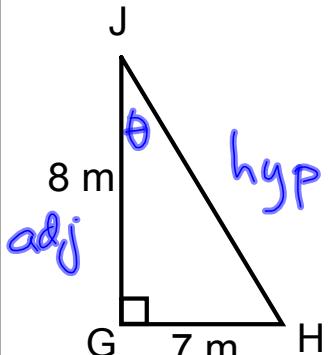
$$\begin{aligned}x &= 12 \cos 52^\circ \\x &\approx 12(0.6157) \\x &\approx 7.3884\end{aligned}$$

$$x \approx 7.4$$

$$x \approx 7.4$$

Dec 9-9:41 PM

Ex.2 Determine the measure of angle J in the triangle shown below.



Soh Cah Toa

$$\tan \theta = \frac{7}{8}$$

$$\tan \theta = 0.875$$

$$\theta = \tan^{-1}(0.875)$$

$$\theta \doteq 41.185^\circ$$

$$\boxed{\theta = 41.2^\circ}$$

$$\tan \angle J = \frac{7}{8}$$

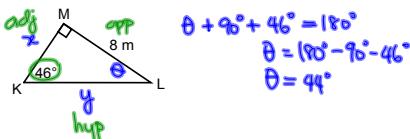
$$\tan J = \frac{7}{8}$$

May 11-3:47 PM

To solve a triangle means to find all the missing sides and angles.

For right triangles use Pythagorean Theorem and/or the primary trigonometric ratios.

Ex.3 Solve the triangle shown below.



$$\begin{aligned} \theta + 90^\circ + 46^\circ &= 180^\circ \\ \theta &= 180^\circ - 90^\circ - 46^\circ \\ \theta &= 44^\circ \end{aligned}$$

Soh Cah Toa

$$\tan 46^\circ = \frac{8}{x}$$

$$x + \tan 46^\circ = 8$$

$$\frac{x(1.0355)}{1.0355} = \frac{8}{1.0355}$$

$$x \doteq 7.7257$$

$$\boxed{x \doteq 7.7}$$

$$\left. \begin{array}{l} y^2 = x^2 + 8^2 \\ y^2 = (7.7257)^2 + 64 \\ y^2 = 123.6864 \\ y \doteq 11.1032 \\ \boxed{y \doteq 11.1} \end{array} \right\} \begin{array}{l} \sin 46^\circ = \frac{8}{y} \\ y \sin 46^\circ = 8 \\ y = \frac{8}{\sin 46^\circ} \\ y \doteq 11.1213 \\ \boxed{y \doteq 11.1} \end{array}$$

May 11-3:58 PM

Assigned Work:

p. 403-406 #1a, 2a, 3, 5a, 6a, 7a, 8a, 10, 12, 13ab

May 11-4:03 PM

6(a)

$\theta$

$a = 10$  adj

$b$

$c = 10$  opp

$a = 10$

$c = 10$

~~Soh Cah Toa~~

$$\tan \theta = \frac{10}{10}$$

$$\tan \theta = 1$$

$$\theta = \tan^{-1}(1)$$

$$\theta = 45^\circ$$

Dec 13-9:12 AM

10.

Similar Δ's  
Pythagorean  
isosceles Δ's

opp      hyp  
adj

$\cos 60^\circ = \frac{4}{i}$

$i \cos 60^\circ = 4$

$i = \frac{4}{\cos 60^\circ}$

$i = \frac{4}{0.5}$

$i = 8$

$\tan 60^\circ = \frac{j}{4}$

$4 \tan 60^\circ = j$

$j = 4(1.732)$

$j = 6.9282$

$j = 6.9$

∴ Side  $i$  is 8cm and  $j$  is 6.9cm

Dec 13-9:22 AM

13. (a)

$x^2 = 8^2 + 5^2$

$x^2 = 64 + 25$

$x^2 = 89$

$x = \sqrt{89}$

$x = 9.4339$

$x = 9.4\text{mm}$

$\tan \theta = \frac{5}{8}$

$\tan \theta = 0.625$

$\theta = \tan^{-1}(0.625)$

$\theta \approx 32.005^\circ$

$\boxed{\theta \approx 32^\circ}$

$\alpha = 180^\circ - 90^\circ - 32^\circ$

$\boxed{\alpha \approx 58^\circ}$

Dec 13-9:30 AM