

Modelling with Trigonometric Functions

Nov. 3/2014

Given data in some form (e.g., graph, table of values, descriptive text), it is possible to model the data as an equation.

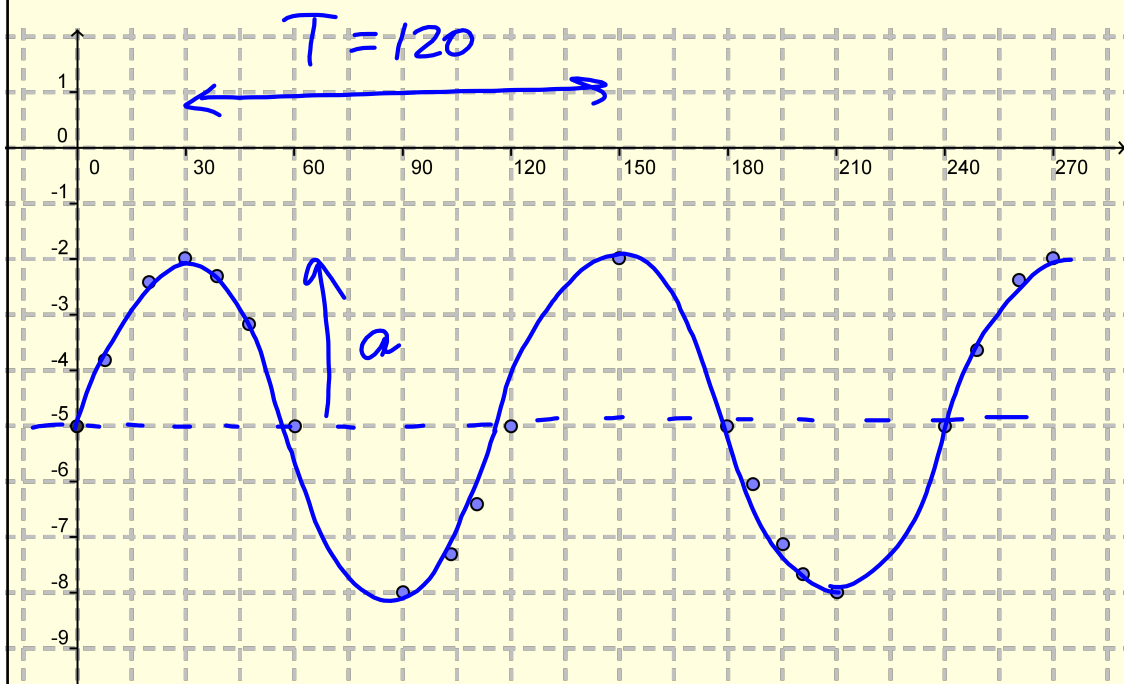
Such models are usually approximations of the actual situation, but they are much simpler to work with than the original data.

They may also have limited applicability, which we express through restrictions on the domain (e.g., an equation may only be valid for the first 24 hours).

When answering questions related to the data, it is often useful to use a combination of the mathematical model (equation) as well as the graphical representation, as each has advantages and disadvantages.

Nov 3-9:27 AM

Ex.1 Create an algebraic model from the following data.



Nov 3-10:07 AM

Assigned Work:

p.360 # 1-3, 5, 6, 7, 9, 11

2

$$3\pi = \frac{2\pi}{k}$$

$$k = \frac{2}{3}$$

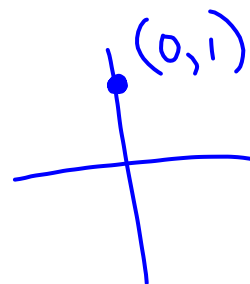
$$2. f(x) = 3 \cos \left[\frac{2}{3} \left(x + \frac{\pi}{4} \right) \right] + 2$$

$$f\left(\frac{\pi}{2}\right) = 3 \cos \left[\frac{2}{3} \left(\frac{\pi}{2} \right) \right] + 2$$

$$= 3 \cos \left[\frac{\pi}{3} \right] + 2$$

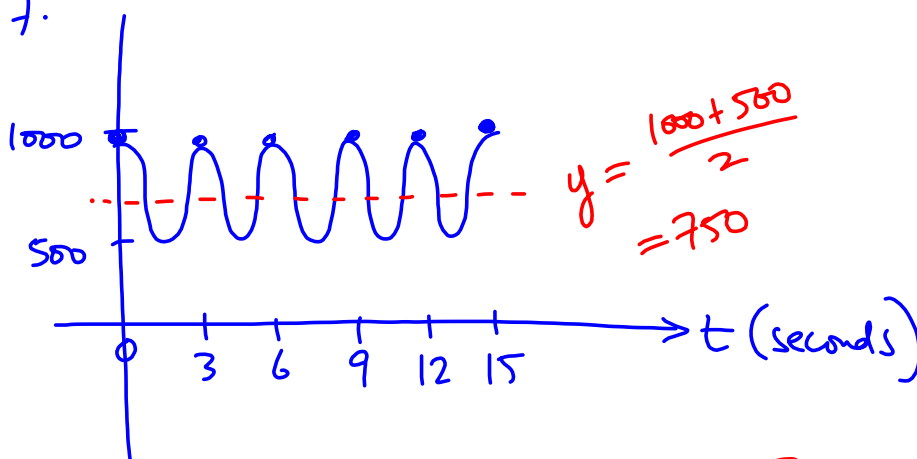
$$= 3(1) + 2$$

$$= 5$$



May 22-8:28 AM

7.



$$T = 3$$

$$p = 0.$$

$$a = \frac{1000 - 500}{2}$$

$$= 250$$

$$\frac{2\pi}{k} = 3$$

$$k = \frac{2\pi}{3}$$

$$f(t) = 250 \cos \left[\frac{2\pi}{3} t \right] + 750$$

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11. $\text{min} = -14.8^\circ\text{C}$ $\text{max} = 17.6^\circ\text{C}$ $\text{AFC: } q = \frac{-14.8 + 17.6}{2}$
 $q = 1.4$
 $|a| = \frac{17.6 - (-14.8)}{2}$
 $|a| = 16.2$

$T(t) = 16.2 \sin\left[\frac{2\pi}{365}(t - 91.25)\right] + 1.4$

Set $T(t) = 0$, solve

$$0 = 16.2 \sin\left[\frac{2\pi}{365}(t - 91.25)\right] + 1.4$$

$$\frac{-1.4}{16.2} = \sin \theta$$

① $\sin RAA = \frac{1.4}{16.2}$ $\text{RAA} = 0.0865$ ② $\frac{S}{A}$

$\theta_1 = \pi + RAA = 3.2281$ $\theta_2 = 2\pi - RAA = 6.1967$

$\frac{2\pi}{365}(t - 91.25) = 3.2281$
 $t - 91.25 = 187.5265$
 $t = 278.8$

OR

$t = 451.2 \leftarrow \text{into 2nd year}$
 $\frac{-365}{86.2} \leftarrow \text{into 1st year}$

\therefore temp below zero
 $t \in [0, 86] \cup [279, 365]$
 1st 86 days of year last 86 days of year.

Nov 4-9:21 AM

9.

falls visible $t_1 \leq t \leq t_2$
 $t_3 \leq t \leq t_4$
 $t_5 \leq t \leq t_6$

$y = -28 \cos\left[\frac{4\pi}{5}x\right] + 28.5$

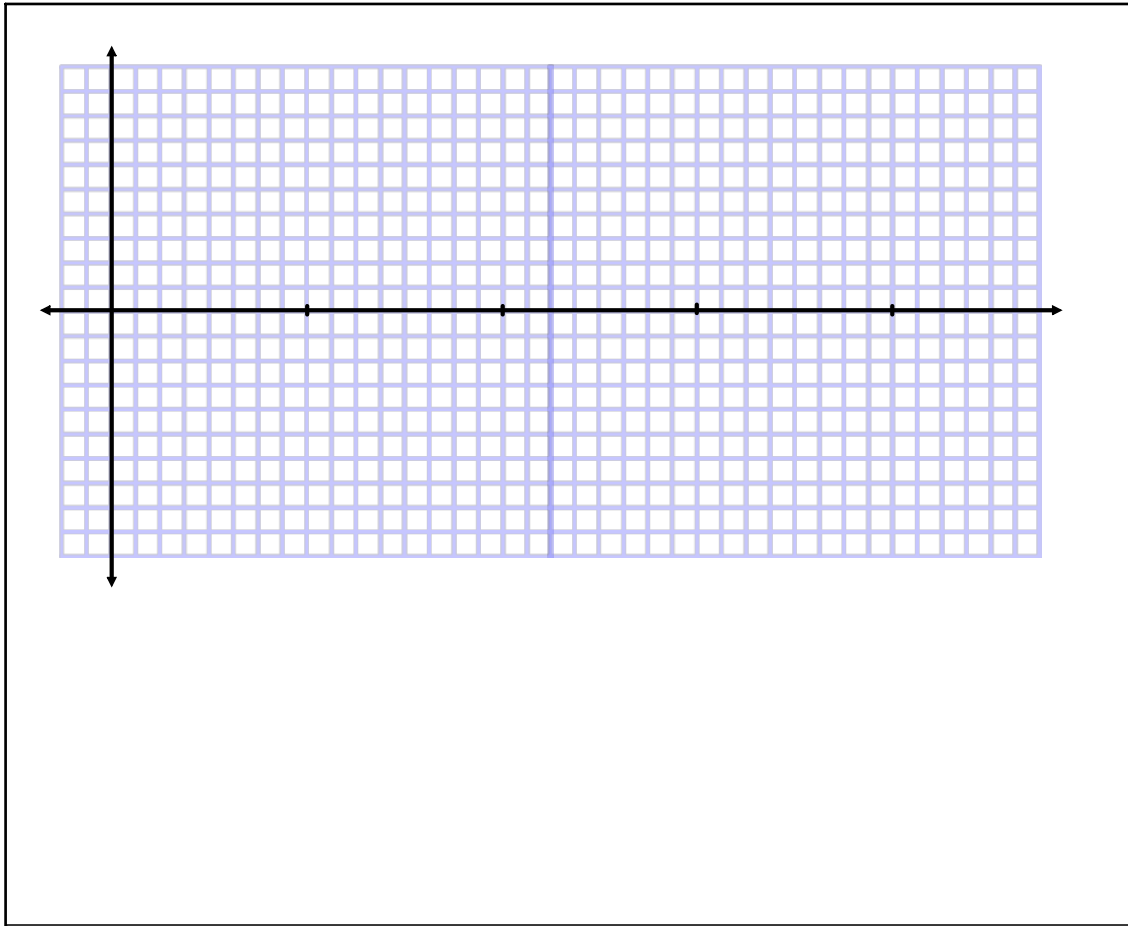
set $y = 50$
 $50 = -28 \cos\left[\frac{4\pi}{5}x\right] + 28.5$
 $21.5 = -28 \cos\left[\frac{4\pi}{5}x\right]$
 $\frac{-21.5}{28} = \cos \theta$

① $\cos RAA = \frac{21.5}{28}$ $\text{RAA} = 0.6953$ ② $\frac{A}{c}$

$\theta_1 = \pi - RAA = 2.4463$ $\theta_2 = \pi + RAA = 3.8369$

$\frac{4\pi}{5}x = 2.4463$ $\frac{4\pi}{5}x = 3.8369$
 $x = 0.97$ $x = 1.53$
 $+ 2.5$ $+ 2.5$
 $+ 2.5$ $+ 2.5$

Oct 31-10:13 AM



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