Suppose you were asked to graph $y = 2^{\sin x}$.

To make matters worse, suppose your calculator could only perform one operation at a time (i.e., you could perform the exponential operation, or the sine operation, but not both).

How would you get the points for your graph?

$$2^{(8)}$$
 $2^{(8)}$ $2^{($

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Composition of Functions

Jan 9/2015

One way to view a function is as a machine, with an input (the independent variable, x) and an output (the dependent variable, y).

$$x \longrightarrow f(x) \longrightarrow y$$
 input machine output

It is possible to connect multiple functions (machines) together, so the output of the first is the input to the second.

$$x \longrightarrow f(x) \longrightarrow y \longrightarrow g(y) \longrightarrow z$$
1st input

1st output

is

2nd output

2nd input

A <u>composition</u> of functions occurs when the <u>argument</u> of a function is another function.

f composed with g

"f of g of x"

outer function inner function (calculate 2nd) (calculate 1st)

Ex.1 Given
$$f(x) = \sqrt{x}$$
 and $g(x) = x^2 - 4$

(a) $(f \circ g)(x)$ (b) $(g \circ f)(x)$

$$= f(g(x))$$

$$= f(g(x))$$

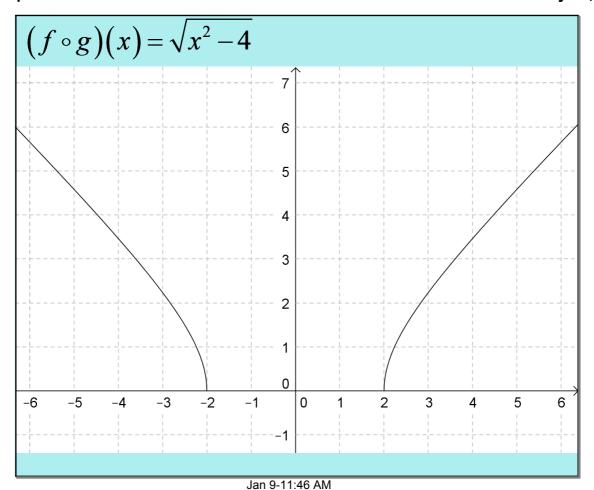
$$= \sqrt{x^2 - 4}, \quad x^2 - 4 \Rightarrow 0$$

$$x^2 \Rightarrow 4$$

$$= x - 4$$

$$x \Rightarrow 0$$

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When determining the domain of $f\circ g$:

- (1) determine the range (output) of g
- (2) determine the domain (input) of f
- (3) restrict the domain of g so its range is within the domain of f

Assigned Work:

p.552 # 1, 2abf, 3, 5aef, 6def, 7cf, 10, 13

$$2(a) (g \circ f)(z) = g[f(z)]$$

$$2 \rightarrow f(z) \rightarrow 5 = g[5]$$

$$5 \rightarrow g(s) \rightarrow 3$$

3.
$$f(q(2)) = f(5)$$

2 = 5

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$$C(x) = 975 + 39.95x$$

$$N(x) = 0.8 C(x)$$

= 0.8 (975 + 39.95x)

$$G(x) = 3x \qquad g(x) = \sqrt{x-4}$$

$$D_{f} = \{x \in \mathbb{R}\} \qquad D_{g} = \{x \in \mathbb{R} | x \neq 4\}$$

$$R_{f} = \{y \in \mathbb{R}\} \qquad R_{g} = \{y \in \mathbb{R} | y \neq 0\}$$

$$(f \circ g)(x) = f(g(x))$$

$$= 3 g(x)$$

$$= 3 (x)$$

$$= 3(x)$$

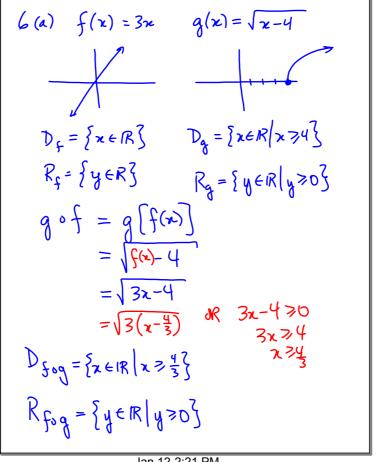
$$x \to g(x) \longrightarrow f(x) \longrightarrow y$$

$$x \neq 4 \longrightarrow y \geq 0$$

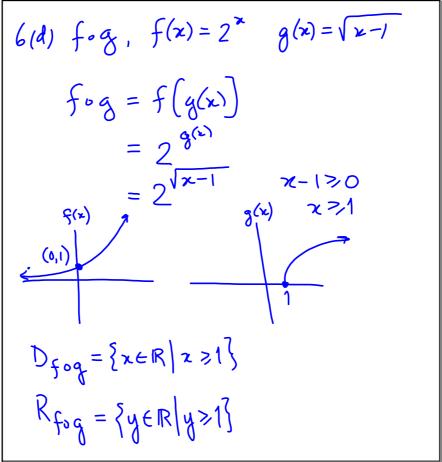
$$D_{f \circ g} \qquad x \neq 0 \longrightarrow y \geq 0$$

$$R_{f \circ g}$$

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